#### Lecture slides for Automated Planning: Theory and Practice

# **Chapter 5 Plan-Space Planning**

Dana S. Nau

CMSC 722, AI Planning University of Maryland, Fall 2004

#### **Motivation**

- Problem with state-space search
  - ◆ In some cases we may try many different orderings of the same actions before realizing there is no solution

dead end — ... — a — b   
dead end — ... — b — a 
$$\rightarrow$$
 c   
dead end — ... — b — a  $\rightarrow$  b  $\rightarrow$  goal   
dead end — ... — a — c  $\rightarrow$  dead end — ... — c — b  $\rightarrow$  a

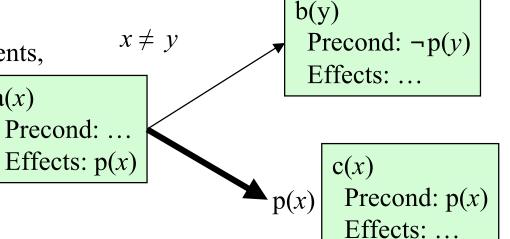
• Least-commitment strategy: don't commit to orderings, instantiations, etc., until necessary

#### **Outline**

- Basic idea
- Open goals
- Threats
- The PSP algorithm
- Long example
- Comments

# Plan-Space Planning - Basic Idea

- Backward search from the goal
- Each node of the search space is a *partial plan* 
  - » A set of partially-instantiated actions
  - » A set of constraints
  - Make more and more refinements, until we have a solution a(x)
- Types of constraints:
  - precedence constraint:a must precede b
  - binding constraints:
    - » inequality constraints, e.g.,  $v_1 \neq v_2$  or  $v \neq c$
    - » equality constraints (e.g.,  $v_1 = v_2$  or v = c) or substitutions
  - causal link:
    - $\Rightarrow$  use action a to establish the precondition p needed by action b
- How to tell we have a solution: no more *flaws* in the plan
  - Will discuss flaws and how to resolve them



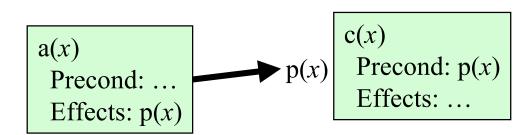
# **Open Goal**

a(*y*)

Precond: ...

Effects: p(y)

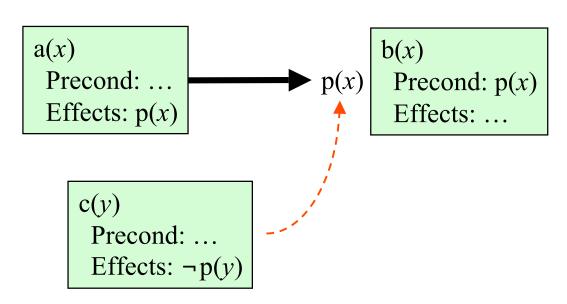
- Flaw:
  - ◆ An action a has a precondition p that we haven't decided how to establish
- Resolving the flaw:
  - Find an action b
    - (either already in the plan, or insert it)
  - that can be used to establish p
    - can precede a and produce p
  - Instantiate variables
  - Create a causal link



c(x)Precond: p(x)Effects: ...

#### **Threat**

- Flaw: a deleted-condition interaction
  - lacktriangle Action a establishes a condition (e.g., p(x)) for action b
  - $\diamond$  Another action c is capable of deleting this condition p(x)
- Resolving the flaw:
  - $\bullet$  impose a constraint to prevent c from deleting p(x)
- Three possibilities:
  - Make b precede c
  - ◆ Make c precede a
  - Constrain variable(s)
     to prevent c from
     deleting p(x)



#### The PSP Procedure

```
\begin{split} & FSP(\pi) \\ & flaws \leftarrow \mathsf{OpenGoals}(\pi) \cup \mathsf{Threats}(\pi) \\ & \text{if } flaws = \emptyset \mathsf{ then } \mathsf{return}(\pi) \\ & \mathsf{select } \mathsf{any } \mathsf{flaw} \ \phi \in flaws \\ & resolvers \leftarrow \mathsf{Resolve}(\phi,\pi) \\ & \mathsf{if } resolvers = \emptyset \mathsf{ then } \mathsf{return}(\mathsf{failure}) \\ & \mathsf{nondeterministically } \mathsf{choose } \mathsf{a} \mathsf{ resolver} \ \rho \in resolvers \\ & \pi' \leftarrow \mathsf{Refine}(\rho,\pi) \\ & \mathsf{return}(\mathsf{PSP}(\pi')) \\ & \mathsf{end} \end{split}
```

PSP is both sound and complete

## **Example**

- Similar (but not identical) to an example in Russell and Norvig's *Artificial Intelligence: A Modern Approach* (1st edition)
- Operators:
  - Start

Precond: none

Effects: At(Home), sells(HWS,Drill), Sells(SM,Milk), Sells(SM,Banana)

Finish

Precond: Have(Drill), Have(Milk), Have(Banana), At(Home)

◆ Go(I,m)

Precond: At(/)

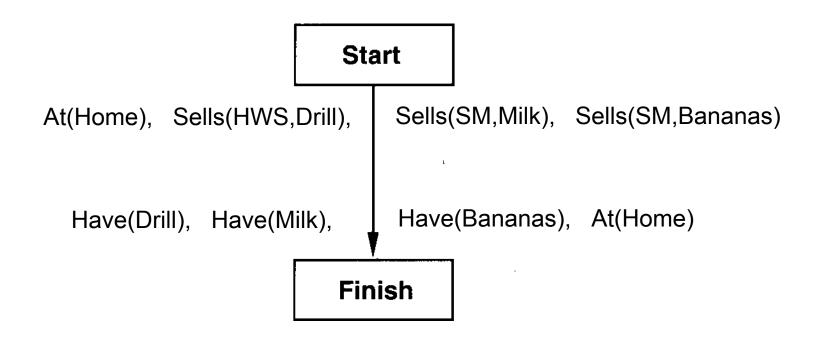
Effects: At(m),  $\neg At(I)$ 

◆ Buy(p,s)

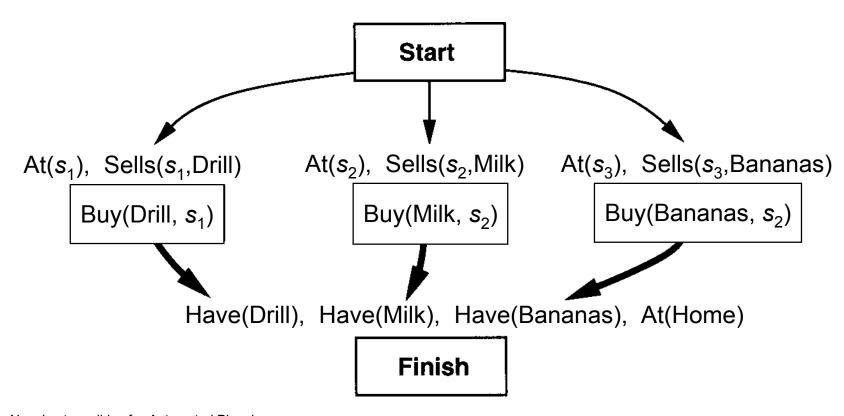
Precond: At(s), Sells(s,p)

Effects: Have(p)

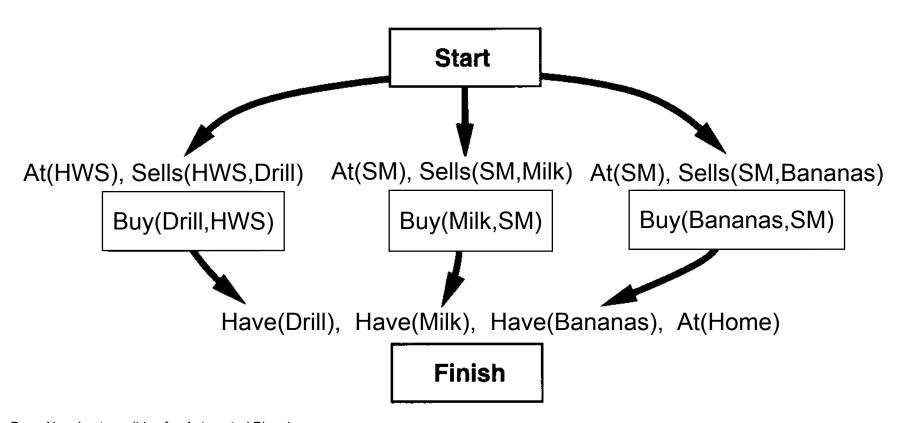
Initial plan



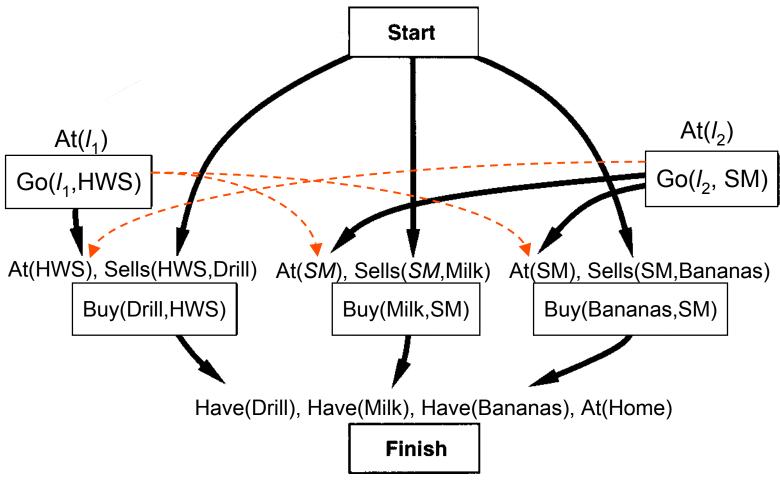
• The only possible ways to establish the "Have" preconditions



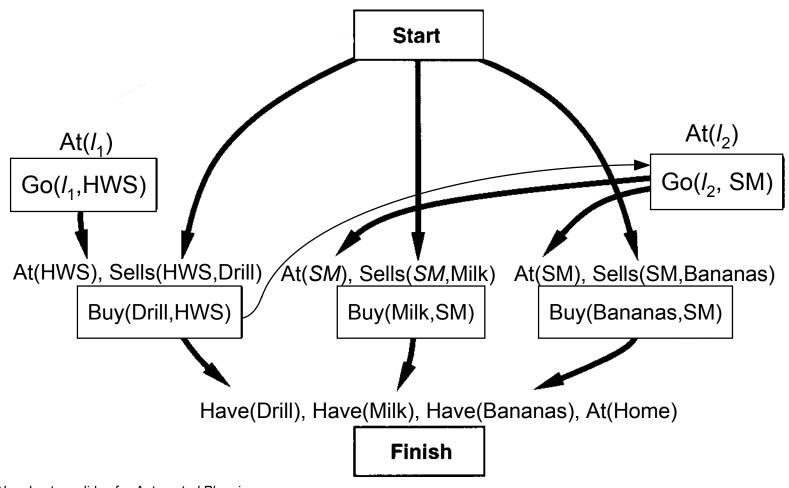
• The only possible way to establish the "Sells" preconditions



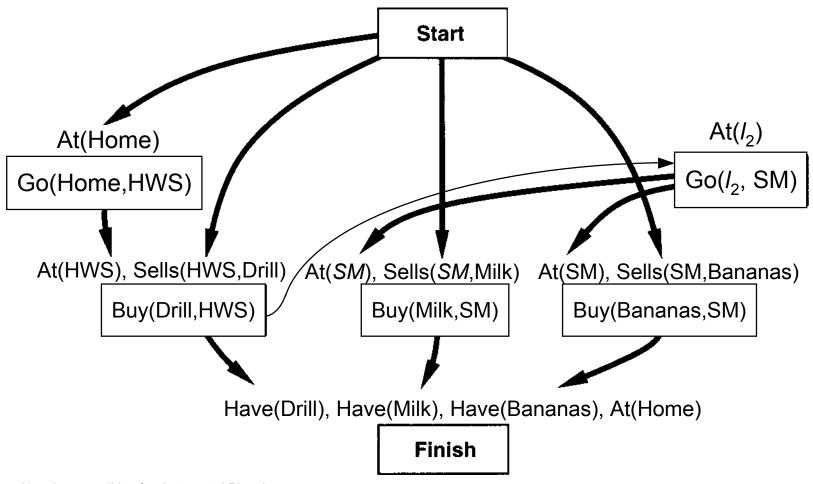
- The only ways to establish At(HWS) and At(SM)
  - ◆ Note the threats



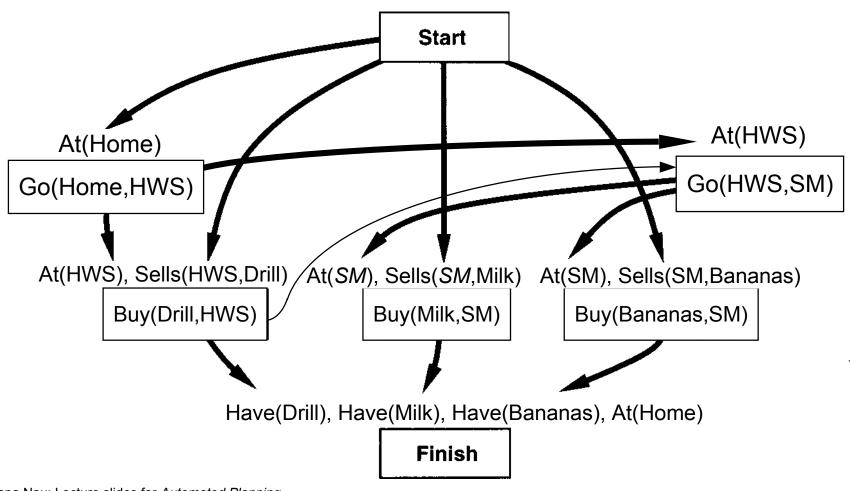
- To resolve the third threat, make Buy(Drill) precede Go(SM)
  - This resolves all three threats



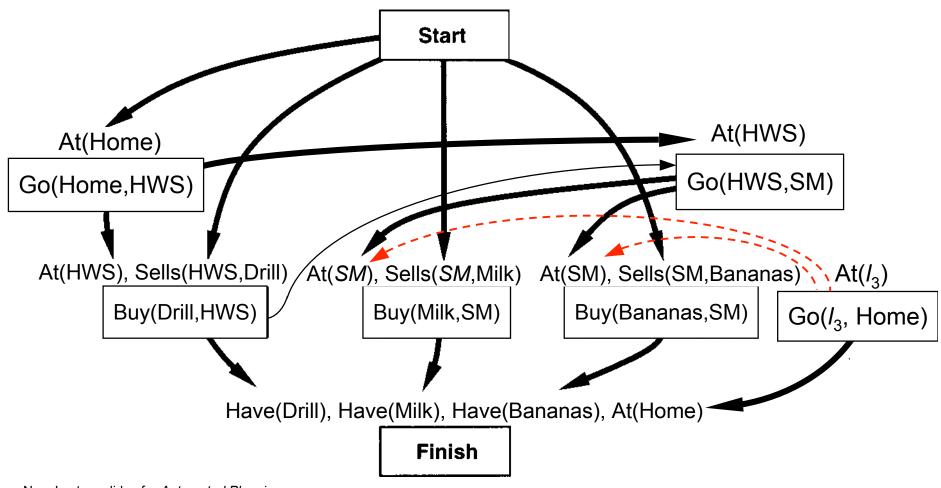
• Establish  $At(l_1)$  with  $l_1$ =Home



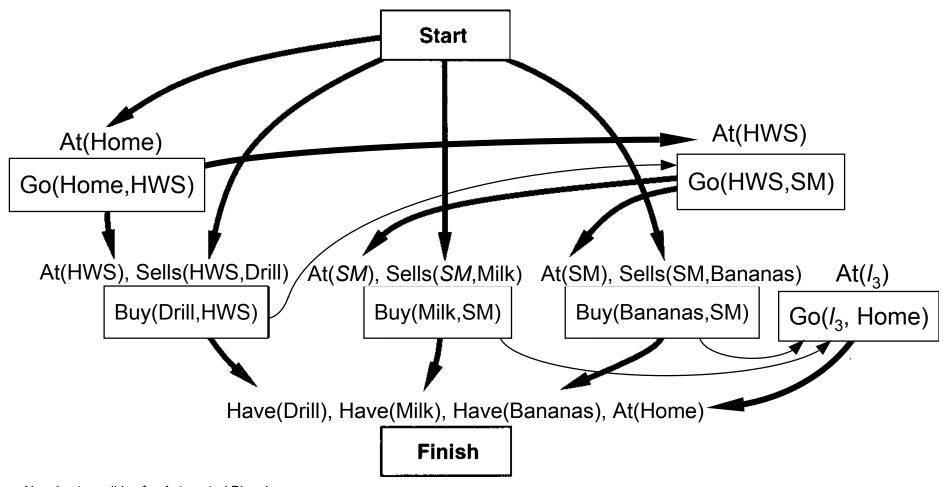
• Establish  $At(l_2)$  with  $l_2$ =HWS



• Establish At(Home) for Finish

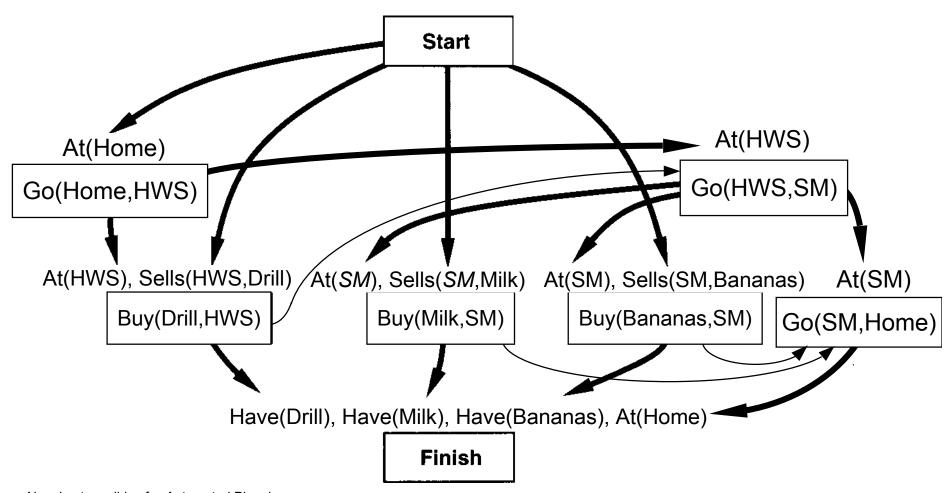


• Constrain Go(Home) to remove threats to At(SM)

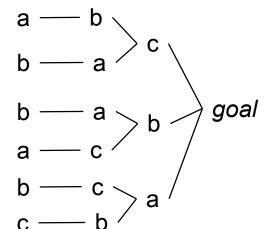


#### **Final Plan**

• Establish  $At(l_3)$  with  $l_3=SM$ 



#### **Comments**



- PSP doesn't commit to orderings and instantiations until necessary
  - ◆ Avoids generating search trees like this one:
- Problem: how to prune infinitely long paths?
  - ◆ Loop detection is based on recognizing states we've seen before
  - ◆ In a partially ordered plan, we don't know the states
- Can we prune if we see the same action more than once?
  ... go(b,a) go(a,b) go(b,a) at(a)
  - No. Sometimes we might need the same action several times in different states of the world (see next slide)

## **Example**

• 3-digit binary counter starts at 000, want to get to 110

$$s_0 = \{d3=0, d2=0, d1=0\}$$
  
 $g = \{d3=1, d2=1, d1=0\}$ 

Operators to increment the counter by 1:

incr0

Precond:  $d_1=0$ 

Effects:  $d_1=1$ 

incr01

Precond:  $d_2 = 0$ ,  $d_1 = 1$ 

Effects:  $d_2=1$ ,  $d_1=0$ 

incr011

Precond:  $d_3=0$ ,  $d_2=1$ ,  $d_1=1$ 

Effects:  $d_3=1$ ,  $d_2=0$ ,  $d_1=0$ 

## A Weak Pruning Technique

- Can prune all paths of length > n, where  $n = |\{\text{all possible states}\}|$ 
  - ◆ This doesn't help very much
- I'm not sure whether there's a good pruning technique for planspace planning