

**DIGITAL GEOMETRY**

**Geometric Methods for Digital Picture Analysis**

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This is the bibliography as published in this book, also containing all corrections which were known by 17 August 2005.

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